**Project & Investment Risk Analysis**

# Variance

* Average of the squared deviations around the mean
* **Symmetrical Measure** → Accounts for deviations **both above and below** the mean





# Semi-Variance

* Investors are typically worried only if their **investment underperforms** thus they are more worried about the **downside risk**
* Average of the squared deviations **strictly above OR below** the mean (**Asymmetrical Measure**)





* 
* 
* 

## Interesting Properties

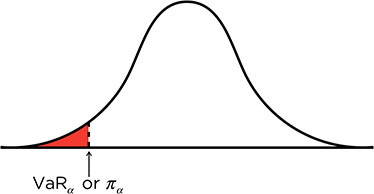
* Variance measures both Upside and Downside risk while semi-variance is just one of the two
  + 
* *F*or a **symmetrical distribution** (Normal & Uniform), the Upside and Downside Variance are **equal**
  + 
  + 

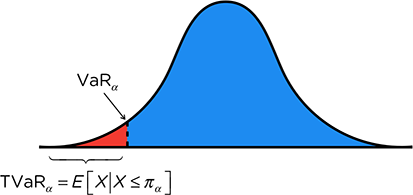
# Value at Risk (VaR)











# Coherence

* There are 4 desirable characteristics for a risk measure
* If a risk measure achieves these 4 targets, then the measure is said to be **Coherent**

|  |  |  |
| --- | --- | --- |
| Name | Expression | Intuition |
| **Translation Invariance** |  | Increasing the risk **increases the risk measure** too |
| **Homogeneity** |  | Scaling the risk **scales the risk measure** too |
| **Subadditivity** |  | Risk Measure **reflects diversification benefits** |
| **Monotonicity** |  | Risk Measure **orders the risk identically** |

|  |  |  |  |  |
| --- | --- | --- | --- | --- |
|  | **Variance** | **Semi-Variance** | **Value at Risk** | **Tail Value at Risk** |
| **Translation Invariance** | No | No | Yes | Yes |
| **Homogeneity** | No | No | Yes | Yes |
| **Subadditivity** | No | No | No  Yes if symmetric | Yes |
| **Monotonicity** | No | No | Yes | Yes |